

Introduction to Physical Science

Quantum Theory
Presented by Robert Wagner

Wave Nature of Particles

- Macroscopic particle has a well-defined momentum ($p = mv$)
- Microscopic world - follow different rules than those for macroscopic objects
 - Light behaves like a particle ; Can an electron behave like a wave
- de Broglie wavelength - electron behaves like a wave
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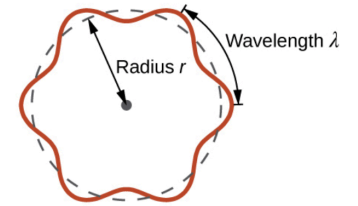


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Electrons as Waves

- Electrons sent through slits create an interference pattern
- Electrons have a dual nature

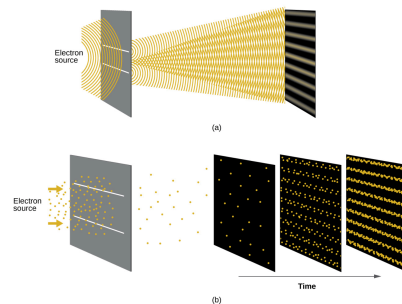


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Example

- If an electron travels at a velocity of $1.00 \times 10^7 \text{ m/s}$ and has a mass of $9.109 \times 10^{-31} \text{ kg}$, what is its wavelength?

$$v = 1.00 \times 10^7 \text{ m/s}; m = 9.109 \times 10^{-31} \text{ kg}$$

$$\lambda = \frac{h}{mv}$$

$$\lambda = \frac{6.626 \times 10^{-34} \text{ kg} \cdot \text{m}^2/\text{s}}{(9.109 \times 10^{-31} \text{ kg})(1.00 \times 10^7 \text{ m/s})}$$

$$\lambda = 7.274 \times 10^{-11} \text{ m}$$

Heisenberg Uncertainty Principle

- How accurately can we measure the properties of an electron (or other particle)?
- A limit to how accurately we can measure the position and momentum of an electron simultaneously.
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- Not significant for macroscopic objects
- Gives an ultimate limit on what can be known in science

Principal Quantum Number

- Principal quantum number (shell number)
 - Location of energy level
 - Energy levels $n = 1, 2, 3, \dots$
- Secondary quantum number (angular momentum)
 - Levels: $l = 0, 1, 2, \dots, n-1$
 - Orbitals: $l = 0$ are s orbitals; $l = 1$ are p orbitals; $l = 2$ are d orbitals; f, g, & h for $l = 3, 4, \& 5$

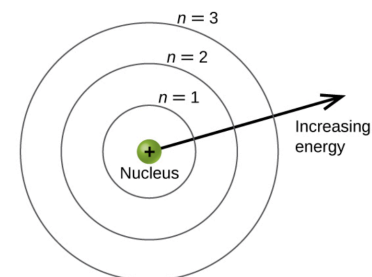


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Quantum Numbers

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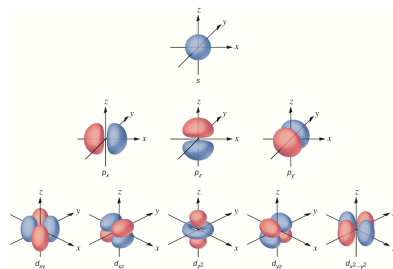


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Quantum Numbers (2)

- Magnetic quantum number
 - Spatial orientation of the orbital
 - Number of orbitals: $2l+1$
- Principal quantum number: General value of electron energy
- Secondary quantum number: Shape of the orbital
- Magnetic quantum number: Orientation of orbital in space

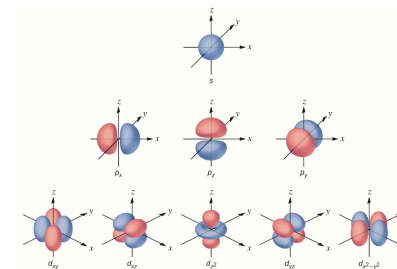


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Orbital Energies

- Orbital is labeled by its principal quantum number and secondary quantum number
- Spin quantum number
 - Electron can have spin "up" or spin "down"

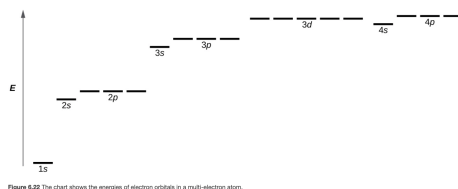


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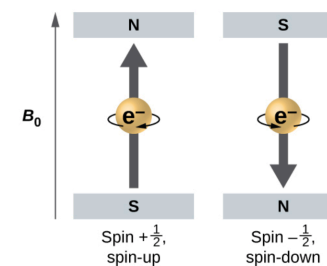


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Pauli Exclusion Principle

- The electron is described by the four quantum numbers.
- Exclusion principle
 - No two electrons in an atom can have the same set of quantum numbers
 - At most two electrons can occupy each orbital

Quantum Numbers, Their Properties, and Significance			
Name	Symbol	Allowed values	Physical meaning
principal quantum number	n	1, 2, 3, 4, ...	shell, the general region for the value of energy for an electron on the orbital
angular momentum or azimuthal quantum number	l	$0 \leq l \leq n - 1$	subshell, the shape of the orbital
magnetic quantum number	m_l	$-l \leq m_l \leq l$	orientation of the orbital
spin quantum number	m_s	$\frac{1}{2}, -\frac{1}{2}$	direction of the intrinsic quantum "spinning" of the electron

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Example

- How many electrons can occupy a shell with $n=2$? $n=5$?

$$n = 2 ; n = 5$$

$n = 2$ has four orbitals: one 2s orbital and 3 2p orbitals. Two electrons per orbital means 8 electrons.

$n = 5$ has 25 orbitals: one 5s orbital, three 5p orbitals, five 5d orbitals, seven 5f orbitals, nine 5g orbitals. Two electrons per orbital means 50 electrons in the shell.

Example

- Complete the table for atomic orbitals.

- n = primary quantum number
- l = secondary quantum number (s,p,d,f,...)
- $m_l = 2l + 1$

Orbital	n	l	m_l degeneracy
4f			
	4	1	
	7		7
5d			

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Summary

- Electrons (and other particles) have been found to behave like waves much as light can behave like a particle
- The uncertainty principle limits how accurately we can know the position and momentum of a particle simultaneously
- Four quantum numbers specify the state of an electron within an atom