5.11: Solid-state NMR

The well-established method of liquid-state nuclear magnetic resonance also suffers challenges when dealing with membrane proteins. In a typical liquid-state NMR experiment, a highly resolved spectrum is obtained due to the fast tumbling, or short correlation times \((\tau_c)\), of molecules that average anisotropic interaction to zero. Only isotropic interaction with the external magnetic field such as scalar couplings remains that makes assigning peaks to individual nuclei and their neighbors possible. However, membrane protein must be embedded into detergent micelles, lipid bicelles, or lipid nanodiscs for liquid-state NMR. The large size of these vehicles dramatically increases the correlation time, thus anisotropic effect such as chemical shift anisotropy and through space dipolar coupling cannot be diminished. The non-averaged proton-proton dipolar interactions result in a featureless single broadband in the chemical shift that can span 25 kHz in width for proton NMR.

Despite the disadvantage of anisotropy interaction in slow or non-tumbling molecules that leads to broad bands in NMR spectra, the broadband can be used to decode the anisotropic information of the molecules. In solid-state NMR (ssNMR), the anisotropic interactions in condensed phases including chemical shift anisotropy (CSA), internuclear dipolar coupling, quadrupolar interaction, and anisotropic J-coupling are studied. The sample size of solid-state NMR can vary from protein microcrystals to complexes like biofilms, intact membranes and even whole cells.
Electron surrounding the nucleus can shield the external magnetic field, disturb the Zeeman interaction, and lead to chemical shift. However, the electron cloud is not spherically distributed due to different bonding anisotropy. The anisotropy of a more asymmetrical functional group like the carbon of carbonyl is more significant than a symmetrical functional group like the carbon of methyl. Different orientations with respect to the applied external field, $B_0$, will have different chemical shift within the same nucleus and appear as a broadband. For example, the bandwidth, $\Delta \sigma$, of a broadband spectrum observed in unoriented phospholipid bilayer can correspond to $\Delta \sigma = \sigma_\parallel - \sigma_\perp$, where $\sigma_\parallel$ is the chemical shift of bilayer oriented parallel to the external magnetic field and $\sigma_\perp$ is the chemical shift perpendicular to the external magnetic field. The $\Delta \sigma$ encodes qualitative viscosity and specific orientation of the membrane molecule. This technique is frequently used to study membrane proteins made up of primarily transmembrane helices.

Nuclei with spin greater than zero have a dipole moment. A nucleus with a dipole moment couples to another nucleus with nuclear spin $I = \frac{1}{2}$ will appear as a doublet in the spectra. The splitting between two maxima can be calculated according to:

$$\Delta v_D(\alpha) = \frac{\mu_0}{4\pi} \frac{\gamma_i \gamma_j}{r_{ij}^3} \frac{\hbar}{2\pi^2} \left(\frac{3 \cos^2(\alpha) - 1}{2}\right)$$

where $\mu_0$ is the permeability of vacuum, $\gamma_i$ and $\gamma_j$ are the gyromagnetic ratios of the nuclei, $r_{ij}$ is the internuclear distance, $\hbar$ is the Planck’s constant, and $\alpha$ is the angle between the vector linking two nuclei and the external magnetic field, $B_0$. In a solid powder sample, each orientation of the dipolar interaction results in a set of doublet, by integrating every orientation, a Pake pattern will appear. If the internuclear distance remains the same but the molecule is fluctuating around an average angle, $\alpha_0$, the equation should be rewritten as:

$$\Delta v_D(\alpha_0) = \frac{\mu_0}{4\pi} \frac{\gamma_i \gamma_j}{r_{ij}^3} \frac{\hbar}{2\pi^2} \left\langle\frac{3 \cos^2(\alpha) - 1}{2}\right\rangle$$

where the term inside the brackets represents the probability distribution of the angle over the rapid fluctuations. The $\Delta v_D$ reflects internuclear distance, orientation and relative motion of a pair of nuclei, but each of the parameters needs to be determined independently in order to deduce the third parameter. The fluctuations of $\alpha$ around $\alpha_0$ can be minimized by cooling the sample, while internuclear distances can be determined from neutron diffraction measurements. In many cases, $\Delta$...
\( \nu_D \) is very small and even difficult to measure.

Overall, the dipolar interaction of \( ^{13} \text{C}-^1 \text{H} \) provides important information but is relatively weak comparing to \(^2 \text{H}\) quadrupolar couplings\(^5\).

**Quadrupolar Interaction**

A quadrupolar moment exists when nucleus has spin \( I > 1/2 \). The quadrupolar interaction is strong and dominates the Zeeman effect. The most useful nucleus in membrane structure studies is \(^2 \text{H}\) with \( I = 1 \). When a \(^2 \text{H}\) bound to a \(^{12} \text{C}\), the quadrupolar splitting \( \Delta \nu_Q \) can be described as:

\[
\Delta \nu_Q(\alpha) = \frac{3}{2} \chi_Q \left( \frac{3 \cos^2(\alpha) - 1}{2} \right) \label{3}
\]

where \( \chi_Q \) is the quadrupolar coupling constant and \( \alpha \) is the angle between the vector linking two nuclei and the external magnetic field, \( B_0 \). In a fluidic membrane system, molecules can rotate around the bilayer normal very rapidly so that the effective averaged symmetry axis of the quadrupolar moment is parallel to the bilayer normal. The \( \Delta \nu_Q \) can be rewritten as:

\[
\Delta \nu_Q(\beta) = \chi_Q \left\langle \frac{3 \cos^2(\alpha) - 1}{2} \right\rangle \left( \frac{3 \cos^2(\beta) - 1}{2} \right) \label{eq4}
\]

where \( \beta \) is the angle between the bilayer normal and the external magnetic field and \( \theta \) is the instantaneous angle between the \(^{12} \text{C}-^2 \text{H}\) bond and the bilayer normal as shown in the following Figure.

![Figure \( (\text{PageIndex}{2}) \). Definition of angles used in equations.](image)

If the bilayer normal wobbles around an average angle \( \beta_0 \), the equation can be further derived as:

\[
\Delta \nu_Q(\beta_0) = \chi_Q \left\langle \frac{3 \cos^2(\alpha) - 1}{2} \right\rangle \left\langle \frac{3 \cos^2(\beta) - 1}{2} \right\rangle \]

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where the term inside the brackets represent the time average of the fluctuations and wobbling and is called the segmental order parameter $S_{CD}$.

\[ ([S_{CD}] = \left\langle \frac{3 \cos^2 (\theta) - 1}{2} \right\rangle \left\langle \frac{3 \cos^2 (\beta) - 1}{2} \right\rangle = S_{fluc} \cdot S_{wob}) \]

The $\Delta \nu_Q$ can be more complicated if the rapid motion of the quadrupolar moment does not have an axial symmetry, or if $^{14}\text{N}$ is involved in the quadrupolar interaction.

The line shape of the solid-state NMR provides orientational information. For slow motion with correlation time larger than $1/\chi_Q$, the linewidth will remain the same while the line shape is distorted. For fast motion such as sonicated membrane vesicles, the line shape can be narrow down to only one line.

Despite the important dynamic parameter $S_{CD}$ can be obtained from the quadrupole splitting, the segmental order parameters in lipids cannot directly infer to the structural information. To obtain a complete average structure of a molecule, the whole order matrix, which contains nine elements, need to be determined. Without complete matrix, the spectra can only provide probabilities and boundaries of conformation in a model-independent fashion. That is why segmental order parameters in lipids are often stated in an elusive term such as “probabilities of being in the trans conformation”.

**J-Coupling**

J-coupling, or scalar coupling, is a through chemical bond isotropic interaction. It is an indirect dipole-dipole interaction mediated by the local electrons between two nuclear spins. J-coupling provides information about the connectivity of molecules, bond distance, and bond angles. The intensity of J-coupling is relatively weak compared to the anisotropic dipolar or quadrupolar interactions.

**Magic-Angle Spinning**

The most commonly used technique in solid-state NMR is Magic-Angle Spinning (MAS). It was proposed by E. R. Andrew, A. Bradbury, and R. G. Eades in 1958, and by I. J. Lowe in 1959. Since the anisotropic interactions include the $(3 \cos^2 (\theta) - 1)$ term, by spinning the sample at the angle $\theta = 54.74^\circ$ where $\cos^2 (54.74^\circ) = 1/3$ one can minimize both the anisotropic interactions and leave only the isotropic interaction. This angle is coined “Magic-Angle” and the method is termed “Magic-Angle Spinning” by Cornelis J. Gorter at the AMPERE congress in Pisa in 1960.

The MAS can dramatically reduce the peak broadening due to anisotropic interaction and give a better resolution of the spectrum for further analysis and identification of the structure.
By placing molecules at the angle of $54.74^\circ$, each bonding might have a different orientation, $\Delta \theta$, with respect to the Magic-Angle, but after applying a rapid spinning around it, the orientation of all the dipolar moments will average to the Magic-Angle as shown in the following Figure.

![Magic angle spinning](image)

Figure \(\PageIndex{3}\). Magic angle spinning to remove anisotropic interaction.

The spinning probe is propelled by air or nitrogen gases with the rotational frequency ranging from 1 to 130 kHz. When the spinning frequency is greater than the width of the static line, the chemical shift anisotropy can also be averaged to zero. The quadrupolar interaction is the strongest anisotropic interaction ($170 \text{ kHz for } ^{12}\text{C-}^2\text{H bond}^{14}$), therefore it requires a very high spinning frequency to remove the quadrupolar coupling, leaving only isotropic J-coupling in the spectra.

**Sensitivity Enhancement**

The sensitivity of solid-state NMR can be enhanced by various techniques. Like the ordinary liquid phase NMR, a higher magnetic field can increase the Zeeman effect and increase the net magnetization due to Boltzmann distribution, thus increasing the sensitivity of NMR signal. Dynamic nuclear polarization (DNP) $^{15}$ is also a popular method in both liquid and solid-state NMR. The basic of DNP is very much similar to Nuclear Overhauser Effect (NOE) but the saturation transfer is from electron to nucleus rather than nucleus to nucleus in NOE. Since an unpaired electron is required to be saturated, a diradicals species must be presented near the target nucleus, thus spin-labelled experiments are often required to do the DNP enhancement. The cryoprobe is also a common technique in liquid-state NMR. The coil and signal preamplifier are cooled by liquid nitrogen or a stream of cold helium gas to reduce the electronics thermal noise and reach as much as a four-fold enhancement in signal-to-noise ratio $^{16}$. 

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References


